Proportionally Fair Distributed Resource Allocation in Multiband Wireless Systems

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Abstract—A challenging problem in multiband multicell self-organized wireless systems, such as femtocells/picocells in cellular networks, multichannel Wi-Fi networks, and more recent wireless networks over TV white spaces, is of distributed resource allocation. This in general involves four components: channel selection, client association, channel access, and client scheduling. In this paper, we present a unified framework for jointly addressing the four components with the global system objective of maximizing the clients throughput in a proportionally fair manner. Our formulation allows a natural dissociation of the problem into two subparts. We show that the first part, involving channel access and client scheduling, is convex and derive a distributed adaptation procedure for achieving a Pareto-optimal solution. For the second part, involving channel selection and client association, we develop a Gibbs-sampler-based approach for local adaptation to achieve the global objective, as well as derive fast greedy algorithms from it that achieve good solutions often.

Index Terms—Femtocells, IEEE 802.11 systems, multiband spectrum access, TV white spaces, wireless resource allocation.

I. INTRODUCTION

ANY of the existing and evolving wireless systems operate over spectrum that spans multiple bands. These bands may be contiguous, as in OFDM-based systems, such as current IEEE 802.11-based WLANs (a.k.a. Wi-Fi networks) and evolving fourth-generation LTE cellular wireless systems; or they may be spread far apart, as in multichannel 802.11 systems and in recently proposed wireless broadband networks over TV white spaces (discussed in Section III). A common issue in these multiband systems is how to perform resource allocation among different clients, possibly being served by different access points (APs). This needs to be done so as to efficiently utilize wireless resources—spectrum, transmission opportunities, and power—while being fair to different clients. Furthermore, unlike traditional enterprise Wi-Fi networks and cellular wireless networks, where the placement of APs and their operating bands are arrived at after careful capacity/coverage planning, more and more of the evolving wireless systems are going to be self-organized networks. There is extensive literature on completely self-organized wireless networks, also referred to as ad hoc networks [1], which are often based on 802.11. Even the emerging 4G cellular wireless networks, such as those based on LTE, are going to have a significant deployment of self-organized subsystems: namely, femtocells and picocells [2], [3]. These self-organized (sub)systems will require that resource allocation is performed dynamically in a distributed manner and with minimal coordination between different APs and/or clients.

In this paper, we consider the problem of joint resource allocation across different APs and their clients so as to achieve a global objective of maximizing the system throughput while being fair to users. We focus on achieving proportional fairness, which has become essentially standard across current 3G cellular systems, as well as in emerging 4G systems based on LTE and WiMAX. Thus, the system objective will be to allocate wireless resources, spectrum, and transmission opportunities, so as to maximize the (weighted) sum of the log of throughputs of different clients, which is known to achieve (weighted) proportional fairness.

The combined resource allocation in a multiband multicell wireless system involves four components: Channel Selection, Client Association, Channel Access, and Client Scheduling. The first component, Channel Selection, decides on how different APs share different bands of the spectrum available to the wireless system. The second component, Client Association, allows a client to decide on an AP to associate within its neighborhood that is likely to provide the “best” performance. Once an AP has chosen a channel/band to operate in and a bunch of clients have associated with it, the third component, Channel Access, decides when it should access the channel so as to serve its clients while being fair to other access points in its neighborhood operating in the same channel. The final component, Client Scheduling, decides which of its clients an AP should serve whenever it successfully accesses the channel.

Our approach addresses the four components in a unified framework, where the solutions to different components are arrived at through separation of timescales of adaptation. More specifically, our formulation allows for the optimization problem of maximizing the clients throughput with weighted proportional fairness to naturally dissociate into two subparts, which are adapted at different timescales. Assuming that the channel selection and client association have been performed, we show that the part involving channel access and client scheduling becomes convex, which is also amenable to a distributed adaptation for achieving Pareto-optimal weighed proportional fairness. At a slower timescale, we adapt the channel selection and client association to varying demands.

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and interference. This part is a nonconvex problem in general and, thus, difficult to solve for a globally optimal solution. We develop a Gibbs-sampler-based approach to perform local adaptation while improving the global system objective. The adaptation is randomized, and if done slowly enough, can achieve a globally optimal solution. In practice, however, that may not be always feasible; hence, we derive greedy heuristics from it for channel selection and client association, which though not globally optimal, provide fast and good distributed solutions with limited exchange of information, as the simulation results indicate. Simulations also illustrate that our resource-allocation policies can achieve significantly better performance than state-of-the-art techniques, such as those proposed in [4] and [5].

The paper is organized as follows. Section II gives an overview of related work. Section III describes the multiccil multiband wireless system model and the joint resource allocation problem that we study. Section IV gives an overview of our approach and discusses the separation of problems. The details of our approach and its desirable properties, including convergence to Pareto-optimal proportionally fair allocation, are given in Sections V and VI. The results of simulations are provided in Section VII. Concluding remarks are discussed in Section VIII.

II. RELATED WORK

There is extensive literature addressing one or a subset of the aforementioned four components of wireless resource allocation in the context of different wireless systems—Wi-Fi networks, 3G/4G cellular networks, and more recent, wireless broadband systems over TV white spaces. Due to space limitation, we only discuss a small sample of the results in each of these areas.

Distributed resource allocation has been widely studied for IEEE 802.11-based systems. A number of CSMA-based random-access approaches have been developed to provide differentiated services to clients [6]–[11]. Proportional fairness in multicontention neighborhood has been studied in [12] and [13]. Specifically, [13] has established that Pareto-optimal weighted proportional fairness can be achieved in a distributed manner with minimal exchange of information among contending clients. Our approach for channel access is motivated by [13]; we, however, consider a more general framework that jointly addresses all the four components. Random-access policies that achieve the entire throughput region have been studied under both the protocol model [14] and the physical model [15]. These studies focus on adapting the access probabilities of each link, but do not incorporate the other control components: channel allocation and client association. Multichannel MACs for Wi-Fi networks have been proposed in [16] and [17]. Approximation algorithms for client association control to achieve proportional fairness have been developed in [4] and [18], but they assume that APs do not interfere with each other through a preassignment of orthogonal channels. A framework based on Markov Approximation has been proposed for combinatorial network optimization problems [19]. However, this work requires each node in the system to obtain system-wide performance. Furthermore, it only provides approximation solutions. The work closest to this paper is [4], where the authors have developed Gibbs-sampler-based distributed algorithms for channel selection and client association. Their approach, however, considers different objectives for the two components, neither of which ensures proportional fairness. On the other hand, [20] and [21] have considered the joint optimization for channel selection, user association, and power control and have proposed algorithms that achieve minimum system-wide potential delay, without considering the possibility of time-sharing or random access.

For cellular wireless data systems, a number of centralized approaches for single-cell scheduling to achieve proportional fairness have been developed [22]–[24]. More recently, several intercell interference coordination (ICIC) techniques have been proposed for interference mitigation in LTE-based 4G cellular networks. Specifically, [25] and [26] have developed distributed algorithms for dynamic fractional frequency reuse among interfering macrocells based on limited exchange of interference information over dedicated control links. Given the nonconvexity of the problem, these algorithms aim to achieve a local optimum of the weighted sum of the log of user throughputs, which as mentioned earlier provides proportional fairness, through local estimates of the appropriate gradients. However, in self-organized subsystems of such networks (such as those made of femtocells and picocells), explicit exchange of information may not be feasible [27], and thus, these approaches may not be directly applicable. Reference [28] has considered the problem of jointly achieving proportional fairness and energy efficiency in LTE systems. It considers a different model where interference only causes the data rate to decrease and does not result in packet collisions. Reference [29] also uses the Gibbs sampler approach to address the problem of utility maximization in general wireless networks. However, its approach may result in excessive complexity and long convergence times. In contrast, by leveraging the knowledge of the optimal solution to some of the control components, our policy has much smaller complexity and faster convergence times.

Research on resource allocation in wireless networks operating over fragmented TV white spaces is in a nascent stage. Reference [30] considers a single AP serving multiple clients at the same rate. For this scenario, it addresses three issues: how the AP chooses a suitable band, how a new client detects the AP’s operating band, and how disruptions due to temporal variations, such as caused by wireless microphones, are handled. Some of the limitations of this approach are overcome in [31] by considering a multirate multiradio architecture. It develops a joint strategy for white space selection and client assignment to one of the radios, as well as designs an extension to CSMA to achieve proportional fairness—all for a single-AP scenario. This paper generalizes the setup by considering a system of multiple APs and jointly addressing the four components of resource allocation to achieve the global system objective of maximizing clients throughput in a proportionally fair manner.

III. SYSTEM MODEL

We consider a system with a finite number of APs and clients that can operate in a number of channels. We denote the set of
APs by \( N_i \), the set of clients by \( I \), and the set of channels by \( C \). Each client \( i \) is associated with an AP and is served by that AP. APs are connected to a backhaul network and can communicate with each other over this network. In Section VI, we will show that each AP only needs to communicate a small amount of data with APs that are physically close to it under our approach. Hence, our approach only causes a small overhead on the backhaul network.

In this paper, we use \( i, j, k, l \) to denote clients, and \( n, m, a \) to denote APs. Many variables can be defined from both a client’s perspective and an AP’s perspective. In this case, we use subscript when the variable is defined from a client’s perspective, and use superscript when the variable is defined from an AP’s perspective. For example, \( x_{ij} \) is the value of \( x \) from client \( i \)’s perspective, while \( x^n \) is the value of \( x \) from AP \( n \)’s perspective.

We denote the AP that client \( i \) is associated with by \( n_i \in N_i \), where \( \bigcup_i N_i \) is the set of APs with which client \( i \) can be associated, subject to both privacy settings of APs and the geographical location of the client. Each AP \( n \) is equipped with \( u^n \) radios that can operate in different channels simultaneously, and each client \( i \) is equipped with only one radio. When an AP \( n \) has more than one radio, i.e., \( u^n > 1 \), we can simplify the model by assuming that there are \( u^n \) APs, each with one radio, that are placed at the same place as AP \( n \). Each of these \( u^n \) APs corresponds to one radio of AP \( n \). This procedure allows us to only consider the model in which each AP has one radio and simplifies notations. Our joint resource-allocation approach will ensure that the co-located APs operate on different bands whenever necessary to optimize the system objective. Hence, throughout the rest of the paper, we assume that each AP only has one radio and operates in one channel unless otherwise specified. The channel in which an AP \( n \) is operating is denoted by \( c^n \). APs can switch the channels in which they operate, although such switches can only be done infrequently due to the large overheads. When an AP switches channels, all its clients also switch channels accordingly. Fig. 1 shows an example of such a system with four APs, 13 clients, and two channels. In the figure, each client is connected to the AP with which it is associated. We use a solid line to indicate that the AP is operating in channel 1, and a dashed line to indicate that the AP is operating in channel 2.

We focus on a server-centric scheme where each AP schedules all transmissions between itself and all clients that are associated with it. This scheme can be naturally applied when all transmissions are downlink ones. Even when there are uplink transmissions, it is still applicable to a wide variety of wireless systems that include LTE, WiMAX, and IEEE 802.11 PCF. Later, we will also discuss a fully distributed scheme where clients contend for service from APs, such as in 802.11 DCF.

We assume that time is slotted, with the duration of a time-slot equal to the time needed for a transmission. If an AP \( n \) makes a successful transmission toward client \( i \) in channel \( c \), client \( i \) receives data at rate of \( B_{i,n,c} \) in this slot. Since the characteristics of different channels may be different, \( B_{i,n,c} \) depends on \( c \). We set \( B_{i,n,c} = 0 \) for all \( n \neq N_i \).

Given the emphasis on self-organized networks, we assume that the APs are not synchronized and may interfere with each other. We consider the interference relations using the protocol model [32]. When an AP \( n \) operates in channel \( c \), it may be interfered by a subset \( M^{n,c} \) of APs, if these APs were to also operate in channel \( c \). We let \( n \in M^{n,c} \) for notational simplicity. When the AP \( n \) schedules a transmission between itself and one of its clients over channel \( c \), the transmission is successful if \( n \) is the only AP among \( M^{n,c} \) that transmits in channel \( c \) during the time of transmission; otherwise, the transmission suffers from a collision and fails. We assume that the interference relations are symmetric, i.e., \( m \in M^{n,c} \) if and only if \( n \in M^{m,c} \). Note that since the propagation characteristics of different channels may be different, especially in the case of TV white space access, the subset \( M^{n,c} \) depends on the channel \( c \). This dependency further distinguishes our work from most existing works on multi-channel access where interference relations are assumed to be identical for all channels. To further simplify notation, we also define \( \overline{M}^{n,c} := \{ m \in M^{n,c} \mid c^m = c \} \), which is the set of APs that actually interfere with \( n \) when it operates in channel \( c \). The main difference between \( M^{n,c} \) and \( \overline{M}^{n,c} \) is that the former describes the physical constraints of the system and is independent of the actual channel in which each AP operates, while the latter depends on the channel in which each AP operates. We also define, for each client \( i \), the set of APs that may interfere with an AP that client \( i \) can be associated with as

\[
M_i := \{ m \in N \mid \exists c \in C, n \in N_i \text{ s.t. } m \in M^{n,c} \}.
\]

In the server-centric scheme, each AP is in charge of scheduling transmissions for its clients. When AP \( n \) accesses the channel, it schedules the transmission for client \( i \), where \( n_i = n \), with probability \( \phi_{i,n} \), \( \phi_{i,n} \geq 0 \) and \( \sum_{n_i = m} \phi_{i,n} = 1 \).

Since APs are not coordinated, we assume that they access the channel by random access. Each AP \( n \) chooses a random access probability, \( p^n \). In each slot, AP \( n \) accesses the channel \( c^n \) with probability \( p^n \). The transmission is successful if \( n \) is the only AP in \( M^{n,c} \) that transmits over channel \( c^n \). Thus, the probability that AP \( n \) successfully accesses the channel in a time-slot can be expressed as

\[
p^n = \prod_{m \in \overline{M}^{n,c}} \frac{1 - p^m}{1 - p^n} \prod_{m \in M^{n,c}} (1 - p^m).
\]

Assume that client \( i \) is associated with AP \( n \) and operates in channel \( c_i \), i.e., \( n_i = n \) and \( c^n = c_i \). Since the data rate of client \( i \) when it is served is \( B_{i,n,c} \), and the probability that the AP \( n \)
makes a successful transmission is as in (1), its throughput per
time-slot is

\[
r_i \triangleq B_{i,n,c} \frac{\frac{1}{1-p^n}}{1 - \frac{1}{1-p^n}} \prod_{m \in \mathcal{M}^i, c_m = c} (1 - p^m). \tag{2}
\]

We now discuss an analog model for a fully distributed
scheme where clients contend for the service from APs, which
is applicable to completely distributed scenarios, such as those
based on 802.11 DCF. In this scheme, each client \( i \) contends
for the channel by accessing it with probability \( p_i \) in each
time-slot. Two clients, \( i \) and \( j \), interfere with each other if their
associated APs interfere with each other, that is, \( c^{n_i} = c^{n_j} \)
and \( n_i \in \mathcal{M}^{n_i}, n_j \in \mathcal{M}^{n_j} \). Client \( i \) successfully accesses the channel if
none of the other clients that can interfere with it accesses the
channel simultaneously. Thus, the long-term throughput per
time-slot for client \( i \) is, assuming \( n_i = n \) and \( c^n = c \):

\[
r_i^D \triangleq H_{i,n,c} \frac{p_i}{1 - p_i} \prod_{j \neq i} (1 - p_j).
\]

Finally, we assume that each client is associated with a posi-
tive weight \( w_i > 0 \). We also denote the total weights of clients
associated with AP \( n \) by \( w^n \), i.e., \( w^n := \sum_{i : n_i = n} w_i \). The goal
is to achieve weighted proportional fairness among clients, that
is, to maximize \( \sum_{i \in \mathcal{C}} w_i \log r_i \). In the fully distributed scheme, the goal is to maximize \( \sum_{i \in \mathcal{C}} w_i \log r_i^D \).

As a final remark, in a dynamic system, the APs and clients
may update their values of different parameters, such as \( n_i, \)
\( c^n, p^n \), etc., with time. However, for simplicity, we omit their
dependence on time from the notation. Throughout this paper,
these variables should be interpreted as their current values.

IV. SOLUTION OVERVIEW AND TIMESCALE SEPARATION

We now give an overview of our approach to achieve
weighted proportional fairness, which consists of decomposing
the problem into four components and solving them. The
solution to the fully distributed scheme is very similar to
that to the server-centric scheme. Thus, we will focus on the
server-centric scheme and only report the key differences of
the fully distributed scheme.

By (2), we can formulate the problem of achieving weighted
proportional fairness as the following optimization problem:

\[
\begin{align*}
\text{max} & \quad \sum_i w_i \log r_i^D \\
- \quad & \sum_i w_i \left[ \log H_{i,n_i,c^{n_i}} + \log \phi_{i,n_i} + \log \frac{p^n}{1 - p^n}, \\
+ \quad & \log \prod_{m \in \mathcal{M}^{n_i}, c_m = c} (1 - p^m) \right].
\end{align*}
\]

s.t. \( c^n \in \mathcal{C}, \) for all \( n \)
\( n_i \in \mathcal{N}, \) for all \( i \)
\( 0 \leq p^n \leq 1, \) for all \( i \)
\( \phi_{i,n_i} > 0, \) for all \( i \)
\( \sum_{i : n_i = n} \phi_{i,n_i} = 1, \) for all \( n. \)

Based on this formulation, the problem of achieving weighted
proportional fairness consists of four important components, in
increasing order of timescales. First, whenever the AP accesses
the channel, it needs to schedule one client for service. That
is, the AP has to decide the values of \( \phi_{i,n_i} \). Second, in each
time-slot, the AP has to decide whether it should access the
channel, which consists of determining the values of \( p^n \). Third,
each client needs to decide with which AP it should be associ-
ated, i.e., deciding \( n_i \). Finally, each AP \( n \) needs to choose a
channel, \( c^n \), in which to operate. We denote the four components
as Scheduling Problem, Channel Access Problem, Client Asso-

ciation Problem, and Channel Selection Problem, respectively.

Weighted proportional fairness is achieved by jointly solving
the four components.

The problem of achieving weighted proportional fairness
for the fully distributed scheme can be formulated similarly as
follows:

\[
\begin{align*}
\text{max} & \quad \sum_i w_i \log r_i^D \\
= & \sum_i w_i \left[ \log B_{i,n_i,c^{n_i}} + \log \frac{p_i}{1 - p_i}, \\
+ \log \prod_{j \neq i} (1 - p_j) \right].
\end{align*}
\]

s.t. \( c^n \in \mathcal{C}, \) for all \( n \)
\( n_i \in \mathcal{N}, \) for all \( i \)
\( 0 \leq p_i \leq 1, \) for all \( i \)

This involves three components: the Channel Access
Problem, which chooses \( p_i \) for clients, the Client Association
Problem, and the Channel Selection Problem.

Since the overhead for a client to change the AP it is associ-
ated with and for an AP to change the channel it operates in
are high, solutions to the Client Association Problem and
the Channel Selection Problem are updated at a much slower
timescale compared to solutions to the Scheduling Problem
and the Channel Access Problem. Based on this timescale sep-

eration, we first study the solutions to the Scheduling Problem
and the Channel Access Problem, given fixed solutions to
the Client Association Problem and the Channel Selection
Problem. We will show that, given solutions to the Client
Association Problem and the Channel Selection Problem, there
are closed-form expressions for the optimal solutions to the
Scheduling Problem and the Channel Access Problem. We
then study the solutions to the Client Association Problem and
the Channel Selection Problem, under the knowledge of how
solutions to the Scheduling Problem and the Channel Access
Problem react. Whenever the solutions to the Client Association
Problem and the Channel Selection Problem are updated, the
solutions to the Scheduling Problems and the Channel Access
Problems are also updated according to the optimal closed-form
expressions. Thus, solutions to the Client Association
Problem and the Channel Selection Problem are indeed joint solutions
to all the four components, and their optimal solutions achieve
Pareto-optimal weighted proportional fairness. In addition to
solving the four components, we will show that the solutions
naturally turn into distributed algorithms where each client/AP makes decisions based on local knowledge.

V. SCHEDULING PROBLEM AND THE CHANNEL ACCESS PROBLEM

In this section, we assume that solutions to the Client Association Problem and the Channel Selection Problem, i.e., \( n_i \) and \( c^n \), are fixed.

Since \( n_i \) and \( c^n \) are fixed, values of \( B_{i,n_i,c^n} \) are constant. The optimization problem can be rewritten as

\[
\begin{align*}
\max & \quad \sum_{i \in I} w_i \left[ \log \phi_{i,n_i} + \log \frac{p^n_i}{1 - p^n_i} + \log \prod_{m \in K^{\infty}_{i,n_i,c^n}} \{1 - p^m_i\} \right] \\
- & \sum_{i \in I} w_i \log \phi_{i,n_i} \\
+ & \sum_{n \in \mathbb{N}} \left[ w^n \log p^n + \left( \sum_{m \in K^{\infty}_{i,n_i,c^n}} w^m - w^n \right) \log(1 - p^n) \right],
\end{align*}
\]

s.t. \( 0 \leq p^n_i \leq 1 \), for all \( n \)

\( \phi_{i,n_i} > 0 \), for all \( i \)

\( \sum_{n=1}^{m} \phi_{i,n} = 1 \), for all \( n \)

where \( w^n = \sum_{n=1}^{m} w_{n} \), as defined in Section III. We also define \( z^n := \sum_{n=1}^{m} w_{n} \) to be the total weight of the clients that are associated with APs interfering with \( n_i \), including itself.

This formulation naturally decomposes the optimization problem into two independent parts: maximizing \( \sum_{i \in I} w_i \log \phi_{i,n_i} \), which is the Scheduling Problem, and maximizing \( \sum_{n \in \mathbb{N}} \left[ w^n \log p^n + \left( \sum_{m \in K^{\infty}_{i,n_i,c^n}} w^m - w^n \right) \log(1 - p^n) \right] / p^n \), which is the Channel Access Problem. Thus, we can solve these two problems independently.

We first solve the Scheduling Problem in the following.

**Theorem 1:** Given \( n_i, c^n \), and \( p^n \), for all \( i \) and \( n_i \), \( \sum_{i \in I} w_i \log r_i \) is maximized by \( \phi_{i,n_i} \equiv w_i / w^n \).

**Proof:** We have \( (\partial / \partial \phi_{i,n_i})(\sum_{i \in I} w_i \log r_i) = (w_i / \phi_{i,n_i}) \). Since \( \sum_{i \in I} w_i \log r_i \) is concave in \( \phi_{i,n_i} \) with the condition \( \sum_{n=1}^{m} \phi_{i,n} = 1 \), we have that \( \{w_i / \phi_{i,n_i} - \{|w_i / \phi_{i,n_i}\}, \phi_{i,n_i} = 1\} \), for all \( i \) such that \( n_i = n(j) - n \), at the optimal point. By setting \( \phi_{i,n_i} \equiv w_i / w^n \), the aforementioned criterion is satisfied. The conditions \( \phi_{i,n_i} \geq 0 \), for all \( i \) and \( \sum_{n=1}^{m} \phi_{i,n} = 1 \), for all \( n \), are also satisfied. Thus, the Scheduling Problem is solved by setting \( \phi_{i,n_i} \equiv w_i / w^n \).

We address the Channel Access Problem next. The following is a direct consequence of [13, Theorem 1].

**Theorem 2:** Given \( n_i, c^n \), and \( \phi_{i,n_i} \), for all \( i \) and \( n_i \), \( \sum_{i \in I} w_i \log r_i \) is maximized by \( p^n \equiv w^n / z^n \).

In summary, when the solutions to the Client Association Problem and the Channel Selection Problem, i.e., \( n_i \) and \( c^n \), are fixed, the AP \( n \) should access the channel with probability \( p^n = w^n / z^n \) in each time-slot and should schedule the transmission for its client \( i \) with probability \( \phi_{i,n} = w_i / w^n \) whenever it accesses the channel. In addition to achieving the optimal solution to both the Scheduling Problem and the Channel Access Problem, this solution only requires \( n \) to know the local information of \( w^n \) and \( c^n \) for all AP \( m \) with which it interferes.

Thus, this solution can be easily implemented in a distributed manner.

We now discuss the fully distributed scheme. With the solutions to the Client Association Problem and the Channel Selection Problem fixed, the problem of achieving proportional fairness is equivalent to maximizing \( \sum_{i} w_i \log p_i + (z^n - w_i) \log(1 - p_i) \). A result similar to Theorem 2 shows that the Channel Access Problem is optimally solved by choosing \( p_i = w_i / z^n \).

VI. CLIENT ASSOCIATION PROBLEM AND THE CHANNEL SELECTION

We now propose a distributed algorithm that solves the Client Association Problem and the Channel Selection Problem based on the knowledge of the optimal solutions to the Scheduling Problem and the Channel Access Problem. These two problems are nonconvex, and a locally optimal solution to the two problems may not be globally optimum. Thus, common techniques for solving convex problems are not suitable for these problems. Instead, the proposed algorithm uses a simulated annealing technique that is based on the Gibbs Sampler, see, e.g., [33], which is proven to converge to the global optimum point almost surely. At the end of Section VI-B, we also derive a greedy heuristic that is easier to implement and converges faster. We first introduce the concept of the Gibbs Sampler.

A. Gibbs Sampler

Consider a system that contains a set of \( V \) entities. Each entity \( v \in V \) can be in a state within a state space \( \Lambda = \{\lambda\} \), and we denote by \( X_v \in \Lambda \) the state of entity \( v \). Define the configuration of the system as the vector \( \psi := [X_v, v \in V] \) consisting of the states of all entities in the system. Let \( \Psi \) be the set of all possible configurations.

Define a utility function on the configuration of the system \( U : \Psi \mapsto R \). The Gibbs sampler is a distributed approach that aims to find the configuration that maximizes the utility function.

Using the Gibbs sampler, each entity updates its state over time. The updates can be taken in either synchronously, e.g., each entity updates in a round-robin fashion, or asynchronously, e.g., each entity uses an independent exponential timer. Suppose an entity \( v \) is to make an update at time \( t \). Assume that the configuration of the system at time \( t \) is \( \psi_t \) and denote \( \psi_t(X_{v_i} = \lambda) \) as the configuration where the entity \( v_i \) is in state \( \lambda \) and all entities other than \( v_i \) are in the same states as they are in \( \psi_t \). The entity \( v_i \) then chooses to be in state \( \lambda_i \), and therefore \( \psi_{t+1} = \psi_{t}(X_{v_i} = \lambda_i) \), with probability

\[
\pi_t(X_{v_i} = \lambda_i) = \frac{e^{U(\psi_t, X_{v_i} = \lambda_i)}}{\sum_{\lambda \in \Lambda} e^{U(\psi_t, X_{v_i} = \lambda_i)}} \tag{3}
\]

where \( T_t \) is referred as the temperature of the system and is decreasing in \( t \). If \( T_t \) is chosen so that \( T_t \to 0 \) and \( T_t \log t \to \infty \) as \( t \) goes to infinity, then \( \lim_{t \to \infty} U(\psi_t) = \max_{\psi \in \Psi} U(\psi) \). More discussion on this can be found in [33, Ch. 7].

B. Distributed Protocol

We now apply the Gibbs Sampler for solving the Client Association and the Channel Selection Problem. We call a
joint solution to both the Client Association Problem and the Channel Selection Problem as a configuration of the system. A configuration is thus fully specified by the AP with which each client is associated, and the channel in which each AP operates. As we aim to achieve proportional fairness among the system, the utility of the system under configuration \( \psi_t \), \( U(\psi_t) \), is defined to be the value of \( \sum w_j \log \gamma \); when APs and clients choose their channels to operate in and APs to be associated with according to \( \psi_t \), and apply the optimal solution to the Scheduling Problem and the Channel Access Problem under \( \psi_t \). We then have

\[
U(\psi_t) = \sum w_i \left[ \log B_{i,n;c(n_i)} + \log \frac{w_i}{w_{n_i}} \right] + \sum_{n \in \mathcal{N}} \left[ w_i \log \frac{w_i}{w_n} + (z^n - w^n) \log \frac{z^n - w^n}{z^n} \right].
\]

Finding the joint solution that achieves Pareto-optimal proportional fairness is equivalent to finding the configuration \( \psi_t \) that maximizes \( U(\psi_t) \).

At each time \( t \), either a client or an AP is selected in a random or round-robin fashion. The selected client, or AP, then changes the AP it is associated with, or the channel it operates in, randomly in a manner described in the following paragraphs, while all other clients and APs make no changes. The solutions to the Scheduling Problem and the Channel Access Problem are then updated according to the new configuration.

We now discuss how the selected client, or AP, changes the AP it is associated with, or the channel it operates in, respectively. Let \( \psi_t(n_i = n) \) be the configuration where client \( i \) is associated with AP \( n \), and the remaining of the system is the same as in configuration \( \psi_t \). We can define \( \psi_t(c^n = c) \) for AP \( n \) similarly. If client \( i \) is selected at time \( t \), it changes the AP it is associated with to \( \psi_t(n_i = m) \) with probability \( e^{U(\psi_t(n_i = n))/T(t)} \), where \( T(t) \) is a positive decreasing function. On the other hand, if AP \( n \) is selected at time \( t \), it changes the channel it operates in to \( c \) with probability \( e^{U(\psi_t(c^n = c))/T(t)} \).

It remains to compute the values of \( U(\psi_t(n_i = n)) \) for client \( i \) and \( U(\psi_t(c^n = c)) \) for AP \( n \). We first discuss how to compute \( U(\psi_t(n_i = n)) \). Let \( w_i \) be the total weight of clients, excluding \( i \), associated with AP \( n \). Define

\[
U^0_i(\psi_t) = \sum_{j \neq i} w_j \left[ \log B_{j,n;c(n_j)} + \log \frac{w_j}{w_i} \right] + \sum_{n \in \mathcal{N}} \left[ w_n \log \frac{w_n}{w_i} + (z^n_i - w^n_i) \log \frac{z^n_i - w^n_i}{z^n_i} \right]
\]

which can be thought of as the utility of the system as if the weight of client \( i \) was zero. We then define \( \Delta U^n_i(\psi_t) := U(\psi_t(n_i = n)) - U^0_i(\psi_t) \). Since in the configuration \( \psi_t(n_i = n) \), \( w^n = w^n_i \) for all \( m \neq n \); \( w^n = w^n_i \); \( z^n = z^n_i + w_i \); \( z^n = z^n_i + w_i \); \( m \in \mathcal{M}, c^n \), and \( m \neq n \); \( z^n = z^n_i + w_i \); \( m \in \mathcal{M}, c^n \), and \( m \neq n \); \( z^n = z^n_i + w_i \); otherwise, we have

\[
\Delta U^n_i(\psi_t) = -w_i \left[ \log B_{i,n;c} + \log \frac{w_i}{w^n} + \sum_{m \in \mathcal{M}, c \neq c(n_i)} w_m \log \frac{w_m}{w^n} \right]
\]

where \( \alpha \) is an constant. Since \( (1 + (w_i/A))^A \approx e^{w_i} \) and \( (1 - (w_i/A))^A \approx e^{-w_i} \), the last approximation holds when \( z^n \gg w_i \), which is true in a dense network where the weights of all clients are within the same order.

Suppose a client \( i \) is selected to change its state at time \( t \), at which time the configuration of the system is \( \psi_t \). The probability that \( i \) chooses AP \( n \) to be associated with is

\[
e^{U(\psi_t(n_i = n))/T(t)} \sum_{m \in \mathcal{M}} e^{U(\psi_t(c^n = m))/T(t)} \]

which can be thought of as the utility of the system as if the weight of client \( i \) was zero. We then define

\[
\Delta U^n_i(\psi_t) := U(\psi_t(n_i = n)) - U^0_i(\psi_t) \]

where \( \gamma \) is the normalizer.

To compute the probability of choosing AP \( n \) to be associated with, client \( i \) only needs the values of \( B_{i,n;c} \) for all \( n \in \mathcal{N}, w^n \) and \( z^n \) for all \( m \in \mathcal{M}, c^n \). Thus, this probability can be computed with \( B_{i,n;c} \), meaning that client \( i \) tends to choose the AP that has higher data rate. Second, it decreases with \( z^n \), which is the total weights of clients that interfere with \( n \). Finally, it increases with \( (z^n - w^n)/z^n \), which is the probability that none of the APs that interfere with \( n \) access the channel.
in a time-slot. Thus, this probability jointly considers the three important factors for the Client Association Problem: data rate, interference, and channel congestion.

Next, we discuss the computation of the probability that an AP $n$ should choose channel $c$ to operate in, if it is selected. Let $z_m := \sum_{\psi \in \mathcal{M}^c,n} \psi_n^c$, where $\mathcal{M}^c = \{m \in \mathbb{M} : c \in \mathcal{C} \}$, and $m \neq n$; and $z_m := z_{m,n}$, otherwise, we have

$$U_n^0(\psi) = \sum_{j \in n,n \neq j} w_j \left[ \log B_{j,n,c} + \log \frac{w_j}{w_{j,n}} \right] + \sum_{m \in \mathcal{M}^c,n \neq m} \left[ w_m \log \frac{w_m}{z_m} + \left( z_m - w_m \right) \log \frac{z_m - w_m}{z_m} \right].$$

We then define $\Delta U_n^0(\psi) := U(\psi|c^c = c) - U_0^0$. Since in the configuration $\psi_k(c^c = c)$, $z_m = z_{m,n} + w_n$ if $m \in \mathcal{M}^c$, and $m \neq n$; and $z_m = z_{m,n}$, otherwise, we have

$$\Delta U_n^0(\psi) = \sum_{i \in n,n \neq i} w_i \left[ \log B_{i,n,c} + \log \frac{w_i}{w_{i,n}} \right] + \left( z_n - w_n \right) \log \frac{z_n - w_n}{z_n} + \sum_{m \in \mathcal{M}^c,n \neq m} \left[ w_m \log \frac{z_m}{z_m + w_n} + \left( z_m - w_m \right) \log \frac{z_m - w_m}{z_m + w_n} \right].$$

When an AP $n$ is selected by the Gibbs sampler at time $t$, it changes the channel it operates in randomly, with the probability of switching to channel $c$ proportional to $e^{U_n^0(\psi)|c^c = c)/T(t)} - e^{U_n^0(\psi)}T(t)$, where $T(t)$ is a cooling schedule. We note that to compute $\Delta U_n^0(\psi)$, AP $n$ only needs the values of $B_{i,n,c}, w_i$, for each client $i$ that is associated with $n$, and $z_m$, for all $m \in \mathcal{M}^c$. Thus, $\Delta U_n^0(\psi)$ can also be computed using only local information.

From the above discussion, a distributed protocol based on the Gibbs sampler, referred to as DP, can be designed (see Algorithm 1). In DP, all clients and APs in the system only need to exchange information within their local areas, as they only need local information to compute the probability of choosing an AP to be associated with or a channel to operate in. Thus, DP is easily scalable. Furthermore, DP achieves Pareto-optimal proportional fairness as $t \to \infty$ almost surely by Section VI-A.

In addition to DP, we can also consider a greedy policy (Greedy) that is easier to implement (see Algorithm 2). Greedy works similarly to DP, except that when a client $i$, or an AP $n$, is selected by the sampler, it chooses the AP that maximizes $U(\psi_k(n_i = n))$ to be associated with, or the channel that maximizes $U(\psi_k(c^c = c))$ to operate in, respectively. It is essentially a coordinate ascent approach. As the number of configurations is finite, it is guaranteed to converge to a local optimum. In addition to a simpler implementation, Greedy is also consistent with the selfish behavior of clients. Each client $i$ chooses the AP $n$ that maximizes $B_{i,n,c}/z_n^c \prod_{\psi \in \mathcal{M}^c \neq n} \left( \frac{z^c}{z^c} + w^c \right)$, which is indeed the value of $r_i$ when $i$ is associated with $n$. 

**Algorithm 1:** Distributed Protocol (DP)

1: for $i \in I$
2: $n_i \leftarrow n$, for some arbitrary $n \in N$
3: broadcast values of $n_i$ and $w_i$ to all $n \in N$
4: for $n \in N$ do
5: $c^n \leftarrow c$, for some arbitrary $c \in C$
6: $w^n \leftarrow \sum_{i \in n,n \in N} w_i$
7: for $i : n_i = n,n \in N_i$ do
8: $\psi_{i,n} \leftarrow w_i/w^n$
9: broadcast values of $c^n$ and $w^n$ to all $m \in \mathcal{M}^c$ and all $\{ i, n \in M_i \}$
10: for $n \in N$ do
11: $z^n \leftarrow \sum_{m \in \mathcal{M}^c} w_m - w^n$
12: $p^n \leftarrow w^n/(z^n + w^n)$
13: broadcast the value of $z^n$ to all $m \in \mathcal{M}^c$ and all $\{ i, n \in M_i \}$
14: for $v \in I \cup N$ do
15: choose arbitrary positive numbers $\tau_v$ and $\theta_v$
16: for time $t$ such that $t - \theta_v/\tau_v$ is an integer, for some $v$ do
17: $T_v \leftarrow 1/((\log t)^{1-\epsilon})$, for any fixed $\epsilon > 0$
18: if $v \in I$ then
19: choose $n_v$ randomly, with the probability choosing $n_v$ proportional to $e^{U_n^0(\psi)|c^c = c)}/T(t)$
20: broadcast values of $n_v$ and $w_v$ to all $n \in N_v$
21: for $n \in N_v$ do
22: $w_n \leftarrow \sum_{i \in n,n \in N} w_i$
23: for $i : n_i = n,n \in N_i$ do
24: $\psi_{i,n} \leftarrow w_i/w^n$
25: broadcast values of $c^n$ and $w^n$ to all $m \in \mathcal{M}^c$ and all $\{ i, n \in M_i \}$
26: for $m \in M_i$ do
27: $z^m \leftarrow \sum_{c \in \mathcal{M}^c} w_m - w^m$
28: $p_m \leftarrow w^m/(z^m + w^m)$
29: broadcast the value of $z^m$ to all $o \in \mathcal{M}^c$ and all $\{ i, n \in M_i \}$
30: else if $v \in N$ then
31: choose $c(v)$ randomly, with the probability choosing $c(v)$ proportional to $e^{U_n^0(\psi)|c^c = c)}/T(t)$
32: broadcast values of $c(v)$ and $w^v$ to all $m \in \mathcal{M}^c$ and all $\{ i, n \in M_i \}$
33: for $m \in \mathcal{M}^c$ do
34: $z^m \leftarrow \sum_{c \in \mathcal{M}^c} w^c - w^m$
35: $p_m \leftarrow w^m/(z^m + w^m)$
36: broadcast the value of $z^m$ to all $o \in \mathcal{M}^c$ and all $\{ i, n \in M_i \}$

**Algorithm 2:** Greedy Policy (Greedy)

1: This approach is identical to Algorithm 1 except that, in Steps 19 and 31, the states of clients and APs are chosen by $n_i(v) \leftarrow \arg \max_n \Delta U_n^0(\psi)$ and $c^n \leftarrow \arg \max_c \Delta U_n^0(\psi)$, respectively.
Thus, in Greedy, every client always chooses to associate with the AP that offers the highest throughput.

A similar protocol can also be designed for the fully distributed scheme where clients, instead of APs, contend for channel access. The protocol also uses the Gibbs sampler as in DP. Define $z_{n,i}$, $z_{m,n}$, $U_{n}^{\text{DP}}(\psi_{i})$, $U_{n}^{\text{Greedy}}(\psi_{i})$, $U_{n}^{\text{MinInt-PF}}(\psi_{i})$, and $U_{n}^{\text{MinInt-Wifi}}(\psi_{i})$ similar to those in the server-centric scheme. We can derive that, for the distributed protocol

\[
\Delta U_{n}^{\text{DP}}(\psi_{i}) = -w_{i} \log \left( H_{n,i} + w_{i} \prod_{j \neq i} \frac{z_{n,j} - w_{j} + w_{i}}{z_{n,j} + w_{i}} \right) - z_{n,i}^{n} + w_{i} \frac{z_{n,i}^{n}}{z_{n,i}}
\]

and

\[
\Delta U_{n}^{\text{Greedy}}(\psi_{i}) = \sum_{i,n_{r}=n} w_{i} \log B_{n_{r}} + \sum_{i,n_{r}=n} \left( z_{n,i}^{n} - w_{i} \right) \log \frac{z_{n,i}^{n}}{z_{n,i}} + \sum_{m \neq n} w_{m} \log \frac{z_{m,n}^{m}}{z_{m,n}^{m} + w_{m}}
\]

We close this section by discussing some implementation issues. The Gibbs sampler requires clients and APs to exchange information locally. Many steps in Algorithm 1 involve broadcasting information to nearby clients and APs. In practice, when an AP needs to broadcast information, it can send the information to other APs (and through them to their clients) over the backhaul network, while of course directly broadcasting the information to its own clients. On the other hand, when a client needs to broadcast information, it first transmits the information to its AP, which subsequently broadcasts the same to its other clients, as well as send to other APs over the backhaul network. This ensures that all clients and all APs have the correct values of the current state when they make updates. Finally, as shown in Algorithm 1, the amount of exchange information is limited, and each client or AP only needs to broadcast information to APs and clients that are physically close to itself. Hence, our protocol only causes a small overhead on the backhaul connections.

VII. SIMULATION RESULTS

We have simulated both DP and Greedy algorithms to compare their performances against other state-of-the-art solutions. We present both simulation results for the server-centric scheme and those for the fully distributed scheme.

We first introduce the model of channel characteristics in our simulation. We use the ITU path-loss model [34] to compute the received signal strength between two devices. If two devices operate in a band with frequency $f$, and are $d$ meters apart, the received signal strength of a device by the other is proportional to $(1/f^2 d^\alpha)$, where $\alpha$ is the path loss coefficient and is set to be 3.5.

We adopt the simulation settings in [5], which models 802.11b channels, as the base case and compute the characteristics of other channels accordingly. 802.11b operates in the 2.4-GHz band with bandwidth 22 MHz. The bit rate between a client and an AP is 11 Mb/s if the distance between them is within 50 m, 5.5 Mb/s within 80 m, 2 Mb/s within 120 m, and 1 Mb/s within 150 m. The maximum transmission range of 802.11b channels is hence 150 m. We assume that two APs interfere with each other if the received signal strength of one AP by the other is above the carrier sense threshold, which, as the settings in ns2 simulator, is set to be 23.42 times smaller than the received signal strength at a distance of the maximum transmission range. Using the ITU path loss model, two APs interfere with each other if they are within the interference range, which is $150 \times (23.42)^{1/3.5} = 369$ m for 802.11b channels.

For channels other than 802.11b channels, we assume that each of them can support four different data rates, corresponding to the four data rates of 802.11b channels. Values of each supported data rate is proportional to the bandwidth of the channel. The transmission range of each data rate, as well as the interference range, is computed so that the received signal strength at the boundary of the range is the same as that at the

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<td>6 MHz</td>
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TABLE I

LIST OF WHITE SPACES IN NEW YORK CITY

Fig. 2. Performance comparison for a three-AP system.
boundary of its counterpart in 802.11b channels. For example, consider a channel that operates in frequency 4 GHz with bandwidth 44 MHz. The bit rate between a client and an AP is $11 \times (44/22) \times 22 = 22$ Mb/s if the distance between them is within $50/(4/2.4)^{2/3} = 37.34$ m, 11 Mb/s within 59.75 m, 4 Mb/s within 89.62 m, and 2 Mb/s within 112.03 m. The interference range of this channel is 275.59 m.

For the server-centric scheme, we compare our algorithms, DP and Greedy, against policies that use state-of-the-art techniques for solving the Client Association Problem and the Channel Selection Problem. Specifically, we compare to [4], which proposes a distributed algorithm for performing channel selection so as to minimize total interference among APs. For the Client Association Problem and the Scheduling Problem, we compare with two techniques. The first technique uses a Wifi-like approach where clients are associated with the closest AP and the AP schedules clients so that the throughput of each client is the same. The protocol that applies both [4] and the Wifi-like approach is called MinInt-Wifi. The other technique is one that is proposed in [5], which, under a fixed solution of the Channel Selection Problem, is a centralized algorithm that aims to find the joint optimal solution to the Client Association Problem and the Scheduling Problem that achieves weighted proportional fairness. This technique first relaxes the Client Association Problem by assuming that each client can be associated with more than one APs and formulates the problem as a convex programming problem. It then rounds up the solution to the convex programming problem and finds a solution to the Client Association Problem where each client is associated with only one AP. For ease of comparison, we use the solutions to the relaxed convex programming problem, which is indeed an upper bound on the performance of [5]. The protocol that applies both [4] and [5] is called MinInt-PF.

In each of the following simulations, we initiate the system by randomly assigning channels to each radio of APs. Each client is initially associated with the closest radio, with ties broken randomly. The system then evolves according to the evaluated policies. We compare the policies on two metrics: the weighted sum of the logarithms of throughput for clients, $\sum_{i \in I} w_i \log r_i$, and the total weighted throughput $\sum_{i \in I} w_i r_i$. All reported data are the average over 20 runs. We first discuss the simulation results for a simple system consisting of three APs and two different channels. While this system is simplistic, it offers insights on the behavior of each policy. We then discuss the simulation results for a larger system where the list of available channels is gathered from a real-world scenario.

Consider a system with three APs, each with one radio, that are separated by 75 m and are located at positions (0, 0), (75, 0), and (150, 0). There are 16 clients, all with weights 1.0, and the $i$th client is located at position $(35 + 5i, 0)$. We consider two settings for channels: one with only one 802.11b channel and the other with one 802.11b channel and a channel that operates...
at frequency 16 GHz with bandwidth 50 MHz. This channel can support higher data rates, but has smaller transmission and interference ranges.

Simulation results are shown in Fig. 2. DP and Greedy outperform MinInt-Wifi and MinInt-PF in both evaluated metrics under both 1-channel and 2-channel settings. For the case where there is only one channel, the solutions of the Channel Selection Problem does not have any influence on the results. MinInt-PF does not have good performance because it distributes clients equally to all three APs, which leads to serious contention and collisions within the network. MinInt-Wifi also suffers from the same problem. On the other hand, under DP, all clients are associated with the AP located at (75, 0), and therefore contention is avoided. This result suggests that a desirable algorithm for the Client Association Problem also needs to jointly consider the effects on both the Scheduling Problem and the Channel Access Problem.

For the case where there are two channels, both MinInt-Wifi and MinInt-PF select the APs at (0, 0) and (150, 0) to operate in the channel at frequency 16 GHz with bandwidth 50 MHz and the AP at (75, 0) to operate in the 802.11b channel. This selection is the only one that results in no interference within the network. On the other hand, DP selects the APs at (0, 0) and (150, 0) to operate in the 802.11b channel and the AP at (75, 0) to operate in the other channel. While this selection results in interference between the APs at (0, 0) and (150, 0), DP actually achieves better performance in both metrics. This is because, in our setting, most clients are gathered around the AP at (75, 0), and thus an optimal solution should allow the AP at (75, 0) to operate in a channel with higher data rates. This shows that an algorithm that aims to minimize interference among APs may not be optimal because it fails to consider the geographical distribution of clients. Furthermore, although the performance of Greedy is suboptimal, which is because the Client Association Problem and the Channel Selection Problem are nonconvex, it is actually close to that of DP and is much better than those of MinInt-Wifi and MinInt-PF.

Next, we consider a larger system, consisting of 16 APs that are placed on a 4 × 4 grid. Adjacent APs are separated by 300 m. There are 16 clients uniformly distributed in each of the two sectors [0, 300] × [0, 300] and [600, 900] × [600, 900]; there are nine clients uniformly distributed in each of the two sectors [0, 300] × [600, 900] and [600, 900] × [0, 300]. We consider the TV white spaces available in New York City, NY, USA [31]. The list of available channels is shown in Table I. We consider two settings: an unweighted setting where all clients have weights 1.0, and a weighted setting where weights clients within the region [0, 300] × [0, 900] have weights 1.5 and clients outside this region have weights 0.5.

Simulation results for different numbers of radios that each AP has are shown in Figs. 3 and 4 for the unweighted setting and the weighted setting, respectively. For both the unweighted
and weighted settings, MinInt-Wifi and MinInt-PF are far from optimum. The total weighted throughputs achieved by the two policies are usually less than one third of those achieved by DP under both settings, especially when the number of radios is large. The performance of Greedy is close to optimum, whose weighted total throughputs are more than 82% of those by DP, under all the settings considered.

For the fully distributed scheme, we also compare our algorithms, DP and Greedy, against MinInt-Wifi. Since [5] is not directly applicable to the fully distributed scheme, we cannot compare our algorithms against MinInt-Wifi.

We consider the same system as that considered in the simulations for the server-centric scheme. This system consists of 16 APs, 50 clients, and seven channels. We consider both the unweighted setting and weighted setting.

Simulation results for the fully distributed scheme are shown in Figs. 5 and 6. In both settings, both DP and Greedy outperform MinInt-Wifi, especially when the number of radios that each AP has is large. Thus, for the fully distributed scheme, a solution that jointly considers all the three components—namely, the Channel Access Problem, the Client Association Problem, and the Channel Selection Problem—is also needed. On the other hand, while Greedy is suboptimal, its performance is close to that achieved by DP. The total weighted throughputs of Greedy are at least 80% of those achieved by DP, under all settings considered here.

Finally, we evaluate the convergence speed of DP and Greedy. We consider the server-centric scheme and use the same settings as those in Figs. 3 and 4. Simulation results are shown in Fig. 7, where we present the results for both the cases of when the clients are weighted and are unweighted. In both schemes, Greedy converges very fast. On the other hand, DP converges slowly. Moreover, with a limited number of updates, DP does not always have better performance than Greedy. This suggests that Greedy may be preferable when convergence rate and system stability are important.

VIII. CONCLUSION

We have studied the problem of achieving weighted proportional fairness in multiband wireless networks. We have considered a system that consists of several APs and clients operating in a number of available channels, accounting for interference among APs and heterogeneous characteristics of different channels. We have identified that the problem of achieving weighted proportional fairness in such a system involves four important components: client scheduling, channel access, client association, and channel selection. We have proposed a distributed protocol that jointly considers the four components and achieves weighted proportional fairness. We have also derived a greedy policy based on the distributed protocol that is easier to implement. Simulation results have shown that the distributed protocol outperforms state-of-the-art techniques. The total weighted throughputs achieved by the distributed protocol can be thrice as large as state-of-the-art techniques. Simulation results have also shown that, while being suboptimal, the performance of the greedy policy is actually close to optimum quite often.

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